

CMSC330 Spring 2025 Quiz 1 Solutions

Problem 1: Basics

[Total 4 pts]

	True	False
In OCaml, the terms values and expressions can be used interchangeably	☐	☒
Using mutable variables can cause side effects	☒	☐
Due to OCaml's type constraints, you cannot make a list of functions	☐	☒
fold_left's accumulator cannot be a tuple	☐	☒
fold_left's accumulator can be a list	☒	☐
fold_left's accumulator can be a tuple	☒	☐
In OCaml, the terms values and expressions cannot be used interchangeably	☒	☐
fold_left's accumulator cannot be a list	☐	☒

Problem 2: OCaml Typing and Evaluating

[Total 6 pts]

Give the type for the following functions foo and give what the following function call evaluates to. **If there is a type error in the function**, put "TYPE ERROR" for the type, and put "ERROR" for the evaluation. If the function call causes an error for any reason, put "ERROR" for the evaluation.

(a) [3 pts]

```
let foo x y =
  match x,y with
  | x::xs,y::ys -> y :: xs
  | _ -> [] ;;
```

foo [] [1;2;3] ;;

Type of foo:

'a list -> 'a list -> 'a list

Evaluation:

[]

(b) [3 pts]

```
let foo lst = let total, _ =
  fold_left
  (fun (tot, idx) ele ->
    (tot + ele * idx, idx + 1))
  (0, 0)
  lst in total;;
```

foo [3;6;9] ;;

Type of foo:

int list -> int

Evaluation:

24

(c)

[3 pts]

```
let foo x y =  
  match x,y with  
    x::xs,y::ys -> y :: xs  
  | _ -> (0,0) ;;
```

```
foo [] [1;2;3] ;;
```

Type of foo:

Type Error

Evaluation:

Error

(d)

[3 pts]

```
let foo lst = let total, _ =  
  fold_left  
    (fun (tot, idx) ele ->  
      (tot*ele*idx, idx + 1))  
  (0, 0)  
  lst in total;;
```

```
foo [7;4;23] ;;
```

(e)

[3 pts]

```
let foo x y = match x,y with  
  x::xs,y::ys -> y :: xs  
  | _ -> [9] ;;
```

```
foo [] [1;2;3] ;;
```

Type of foo:

int list -> int

Evaluation:

0

Type of foo:

int list -> int list -> int list

Evaluation:

[9]

(f)

[3 pts]

```
let foo lst = let total, _ =  
  fold_left  
    (fun (tot, idx) ele ->  
      (tot + ele * idx, idx + 1))  
  (0, 0)  
  lst in total;;
```

```
foo [2;4;8] ;;
```

(g)

[3 pts]

```
let foo x y = match x,y with  
  x::xs,y::ys -> y :: xs  
  | _ -> [] ;;
```

```
foo (1,3) [1;2;3] ;;
```

Type of foo:

int list -> int

Evaluation:

20

Type of foo:

'a list -> 'a list -> 'a list

Evaluation:

Error

(h)

[3 pts]

```
let foo lst = let total, _ =  
  fold_left  
    (fun (tot, idx) ele ->  
      (tot * ele * idx, idx + 1))  
  (1, 0)  
  lst in total;;
```

```
foo [1;3;5] ;;
```

Type of foo:

int list -> int

Evaluation:

0

Problem 3: Filter

[Total 4 pts]

`filter` is another common higher order function that has type `('a -> bool) -> 'a list -> 'a list`. It applies a function to every item in a list and returns a list of the items that caused the function to return true. **using only fold (left or right, given below)**, write a function called `my_filter` which has the same functionality as `filter`. `f` will be the function that returns true or false, and `l` will be the list. **Note:** the original order must be maintained.

```
(* example: my_filter (fun x -> x > 3) [2;4;6] = [4;6] *)

let my_filter f l = fold_right (fun x acc -> if f x then x :: acc else acc) l []
----- alternatively -----
let my_filter f l = fold_left (fun acc x -> if f x then acc @ [x] else acc) [] l
```

Problem 4: Coding

[Total 6 pts]

Write a function call `last_sum` which takes in a `int list list` and returns the sum of the last elements in each `int list`. If list is empty, it adds nothing to the total.

You can write helper functions, you may use the `rec` keyword, **you do not have to use map/fold** (however they are still given). You may not use any List module functions, except those provided. (`cons` and `@` are fine). You may also not use any imperative OCaml.

```
(* last_sum has type int list list -> int *)
(* Examples
    last_sum [] = 0
    (* 3 + 6 + 9 *)
    last_sum [[1;2;3];[4;5;6];[7;8;9]] = 18
    (* 0 + 1 + 3 *)
    last_sum [[];[1];[2;3]] = 4
*)

let rec map f l = match l with
  [] -> []
|x::xs -> (f x)::(map f xs)

let rec fold_left f a l = match l with
  [] -> a
|x::xs -> fold_left f (f a x) xs

let rec fold_right f l a = match l with
  [] -> a
|x::xs -> f x (fold_right f xs a)

(* Write your code below *)

let rec last_sum mtx =
  let lasts = map (fun x -> fold_left (fun acc el -> el) 0 x) mtx in fold_left (+) 0 lasts
----- alternatively -----
let last_usm mtx = fold_left (fun a x -> a + (fold_left (fun a x -> x) 0 x)) 0 mtx
----- alternatively -----
let rec get_last lst = match lst with
| [] -> 0
| [x] -> x
| x :: xs -> get_last xs

let rec last_sum mtx = let lasts = map (fun x -> get_last x) mtx in fold_left (+) 0 lasts
----- alternatively -----
let rec last_sum mtx =
  let rec get_last lst = match lst with
    [] -> 0
    | [x] -> x
    | _::xs -> get_last xs in
  match mtx with
  [] -> 0
|x::xs -> get_last x + last_usm xs
```

Write a function call `last_prod` which takes in a `int list list` and returns the product of the last elements in each `int list`. If list is empty, it multiplies the value by 1.

You can write helper functions, you may use the `rec` keyword, **you do not have to use `map/fold`** (however they are still given). You may not use any List module functions, except those provided. (`cons` and `@` are fine). You may also not use any imperative OCaml.

```
(* last_prod has type int list list -> int *)
(* Examples
   last_prod [] = 1
   (* 3 * 6 * 9 *)
   last_prod [[1;2;3];[4;5;6];[7;8;9]] = 162
   (* 1 * 1 * 3 *)
   last_prod [[];[1];[2;3]] = 3
*)
(* Write your code below *)
```

```
let rec map f l = match l with
  [] -> []
  |x::xs -> (f x)::(map f xs)
```

```
let rec fold_left f a l = match l with
  [] -> a
  |x::xs -> fold_left f (f a x) xs
```

```
let rec fold_right f l a = match l with
  [] -> a
  |x::xs -> f x (fold_right f xs a)
```

```
let rec last_prod mtx =
  let lasts = map (fun x -> fold_left (fun acc el -> el) 1 x) mtx in fold_left ( * ) 1 lasts

----- alternatively -----
```

```
let last_prod mtx = fold_left (fun a x -> a * (fold_left (fun a x -> x) 1 x)) 1 mtx

----- alternatively -----
```

```
let rec get_last lst = match lst with
| [] -> 1
| [x] -> x
| x :: xs -> get_last xs
```

```
let rec last_prod mtx = let lasts = map (fun x -> get_last x) mtx in fold_left ( * ) 1 lasts

----- alternatively -----
```

```
let rec last_prod mtx =
  let rec get_last lst = match lst with
    [] -> 1
    | [x] -> x
    | _::xs -> get_last xs in
  match mtx with
  [] -> 1
  |x::xs -> get_last x * last_prod xs
```

Write a function call `last_concat` which takes in a string list `list` and returns the result of concatenating the last elements in each string `list`. If `list` is empty, it should not modify the resulting string.

You can write helper functions, you may use the `rec` keyword, **you do not have to use `map/fold`** (however they are still given). You may not use any List module functions, except those provided. (`cons` and `@` are fine). You may also not use any imperative OCaml.

```
(* last_concat has type string list list -> string *)
(* Examples
  last_concat [] = ""
  (*"b" ^ "d" ^ "f" *)
  last_concat [["a";"b"];["c";"d"];["e";"f"]] = "bdf"
  (* "" ^ "a" ^ "c" *)
  last_concat [[];["a"];["b";"c"]] = "ac"
*)

(* Write your code below *)

let rec map f l = match l with
  [] -> []
|x::xs -> (f x)::(map f xs)

let rec fold_left f a l = match l with
  [] -> a
|x::xs -> fold_left f (f a x) xs

let rec fold_right f l a = match l with
  [] -> a
|x::xs -> f x (fold_right f xs a)

let rec last_concat mtx =
  let lasts = map (fun x -> fold_left (fun acc el -> el) 1 x) mtx in fold_right ( ^ ) lasts ""

----- alternatively -----

let last_concat mtx = fold_left (fun a x -> (fold_left (fun a x -> x) "" x) ^ a) "" mtx

----- alternatively -----

let rec get_last lst = match lst with
| [] -> ""
| [x] -> x
| x :: xs -> get_last xs

let last_concat mtx = let lasts = map (fun x -> get_last x) mtx in fold_right ( ^ ) lasts ""

----- alternatively -----

let rec last_concat mtx =
  let rec get_last lst = match lst with
    [] -> 1
  | [x] -> x
  | _::xs -> get_last xs in
  match mtx with
  [] -> 1
|x::xs -> get_last x ^ last_concat xs
```