Chapter 1

OCaml

We will do so much Ocaml, you could call it Ocamlot

Cleff

This is a programming language chapter so it has two (2) main things: talk about some properties that the OCaml programming language has and the syntax the language has. If you want to code along, all you need is a working version of OCaml and a text editor. You can check to see if you have OCaml installed by running ocaml -version. At the time of writing, I am using Ocaml 4.14.0. ocaml is repl which you can use to play around with OCaml but please use utop. It's a wrapper for ocaml and is much easier to use.

1.1 Introduction

OCaml will probably look (and act) unlike any other language you have come across in the CS department up to this point. This is due to one key difference: OCaml is a declarative programming language, opposed to an imperative language. We will talk about this all in the next section, but for now let's just write our very first program.

```
1 (* helloWorld.ml *)
2 print_string "hello world"
```

Despite this being very simple, we observed five (5) things.

- Comments are surrounded by (* ... *)
- · no semicolons to denote end of statement*
- print_string is used to print things out to stdout
- Parenthesis are optional when calling functions*
- OCaml file name conventions are camlCase.ml
- Strings exists in the language (most languages do, but some do not)

Now you may have noticed the * symbol over point 2 and 4. That is because these observations are actually False. Or at least, not entirely true. For now though, let's just roll with it. In order to have the above code run, you can run

```
ocamlc helloWorld.ml
./a.out
```

Congrats, you have just made your first program in OCaml! There are some things to note however:

• OCaml is a compiled Language

ocamlc is the ocaml compiler (some compilers like to take the name of the language and add 'c' to the end: javac, ocamlc, rustc).

- If you run an ls you will notice that along with the executable a.out, two other files were generated as well, helloWorld.cmo and helloWorld.cmi. The .cmo is the object file and can be thought of as analogous to the .o file generated by gcc. The cmi file is the interface file and can be thought of as analogous a compiled down .h file in c
- ocamlc is wrapped in a nice program called dune. dune will allow you to compile, run, and test your OCaml programs without much overhead. We use dune to help manage your projects.

1.2 Type System

As mentioned in the python/ruby chapters, a type system dictates the how data is treated, along with what you can do with certain pieces of data. To recap, let's first talk about type checking.

Type checking is the process of determining what a piece of data's type is. Should the bitstring 0100000101000001 be treated as a string and have the value of "AA" or should it be treated as an int with the value of 16705? Addittionally, when should this checking occur? At compile time? Runtime? Different type systems have different answers to these questions. Let's first start with then when.

Static typing is something you are familiar with from Java and C: type checking is done at compile time. In Python or Ruby where there is no compiler¹, type checking is done at runtime. This is called dynamic typing. Static and Dynamic typing are contrasting and only dictate *when* type checking should occur. To talk about how types are checked, then we need to talk about other type systems.

Explicit typing is something you are familiar with in Java and C: the programmer must explicitly state the type at creation of the variable.

```
int i = 3;
String s = "hello';
```

The above are examples of explicit typing. This is very important in C because you can do whatever you want with whatever data for the most part. Explicitly typed languages are almost always associated with manifest typing (and sometimes these terms are used interchangeably). With manifest typing, types are associated with variables, not values. Thus, it is the variable i that has type int, and not the bitstring 00000011.

In contrast to this is the idea of implicit typing (sometimes called latent typing), where the programmer does not need to put down the type of the variable. In this case, type inference occurs, where the language will infer the types of the data (we see this in OCaml) and we saw this in Python. In this case, types are associated with values and not variables.

It is important to note, that explicit and implicit type systems are independent of static and dynamic type systems. They do not imply each other. OCaml is a static and implicitly typed language. Python is a dynamic and implicitly typed language. C is a static and explicitly typed language.

1.3 Functional Programming

According to Wikipedia, "functional programming is a programming paradigm where programs are constructed by applying and composing functions". This probably means nothing to you, so let's make our own definition. First let's define a few words, or rather one in particular: paradigm. Depending on the field, it has many different definitions. I don't want to take the lingustic's definitions, despite that is the one used here. I want to take the more general one: a set of thoughts and concepts related to a topic. With this definition, I will say this: Functional programming is a way of programming that focuses on creating functions rather than listing out steps to solve a problem. I'm sure that many people will disagree and dislike this definition but oh well.

¹python does do some compile like things tho

1.3.1 Declarative Languages

Functional languages are typically described as declarative. This means that values are declared and the focus is declaring **what** a solution is, rather than describing **how** a solution is reached. To see this let's do a real quick comparison in English for a process that finds even numbers in a list

Imperative

- + make an empty list called results
- + Look at each item in the list
- + Divide the item by 2 and look at the remainder
- + if the remainder is o, add the value to the results list
- + return the results list after you looked at all list items

Declariative

- + Take all the values that are even divisible by 2 from the list
- + Return those values

Notice that the imperative instructions tell you how to do something and does so in steps. The declarative instructions tells you what you are looking for and assumes you can just figure out how to do it. If we translate the imperative code to Python we get something like

```
1 #imperative.py
2 def evens(arr):
3    results = []
4    for x in arr:
5        remainder = item % 2
6        if remainder == 0:
7        results.push(item)
8    return ret
```

Now we haven't learned enough (or really any) OCaml at this point to write a solution to this yet², but let's look at a declarative python example:

```
1 #declarative.py
2 results = [x for x in arr if x % 2 == 0]
```

Here, we don't tell python how to solve the problem, we tell it what we want and python figures out the rest.

1.3.2 Side effects and Immutability

One thing that functional programming aims to do is to minimize this idea of a side affect. Consider the following Python Code:

```
1  # side_effects.py
2  count = 0
3  def f(node):
4   global count
5   node.data = count
6   count+=1
7  return count
```

Functional programming wants to treat functions as, well, a function. This means that something like the following should be true:

```
f(x) + f(x) + f(x) = 3 * f(x)
```

However, if we run the code above, then f(x) + f(x) + f(x) = 1 + 2 + 3 and 3 * f(x) = 3 * 1. This unpredictability is called a side effect (The true definition of a side effect is when non local variables get modified). When side effects occur, it becomes harder to reason and predict the behaviour of code (which means more bugs!). To combat this, OCaml makes all variables immutable to help maintain **referential transparency**. Referential transparency is the ability to

 $^{^{2}}$ If you wanted a solution here is one: let rec even lst = match lst with []-> []|h::t -> if h mod 2 == 0 then h::(even t) else (even t) in even lst

replace an expression or a function with it's value and still obtain the same output. To simplify, OCaml wants to minimize the amount of outside contact your code has to make everything self contained. The more you rely on outside information or context, the more complicated your code becomes. Now we need to address the question, "What is an expression or function's value?"

1.3.3 Expressions and Values

In functional languages, one of the core ideas is ability to treat functions as data. Which means much like in python, we can pass functions in as arguments, or use them as return values to other functions. But we are getting a little ahead of ourselves. Let's first see what data is in OCaml.

In OCaml, we say that almost everything is an expression. ³Expressions are things like 4 + 3 or 2.3 < 1.5. We say that expressions evaluate to values. A value is something like 7 or false. All values are expressions in and of themselves, but not all expressions are values. Like a square and rectangle situation. All expressions also have a (data) type. The expression 3+4 evaluates to 7 so we say that both expressions have type int. For the purpose of these notes I will use *e* to represent an expression, *t* for type, and the structure *e*: *t* to say that the expression *e* evaluates to type *t*. Consider the following:

```
1 (* expressions.ml *)
2 true: bool (* is a value, has type bool *)
3 3 * 4: int (* is an expression, has type int *)
4 "hello" ^ "world": string (* is an expression of type string *)
5 5.4: float (* a value of type float *)
```

Now, we said that almost everything is an expression but we do have one thing that I would not consider an expression: the binding of expressions to variables.⁴ This can get confusing because there are these things called let *bindings* and let *expressions*. We will talk about the former first.

A let binding just binds an expression to a variable. We cannot use it where we typically expect an expression. Here is an example:

```
1 (* letBinding.ml *)
2 let x = 3 + 4
3 (* syntax *)
4 (* let variable = e*)
```

It is important to note that OCaml uses static and latent typing. Also recall that variables in OCaml are immutable. When we run the above code in a repl like *utop* we are actually setting a top level variable which can be used to refer in other places. We ultimately want to try and avoid this to maintain more strict referential transparency so we have this expression called a let expression.

A let expression is like setting a local variable to be used in another expression.

```
1 (* letExpression.ml *)
2 let x = 3 + 4 in x + 1
3 (* syntax *)
4 (* let variable = e1 in e2 *)
```

In this case, we add the in keyword and follow up with another expression. In this case, this is an expression so it does have a value it will evaluate to and also has a type. It's type is dependent on what the second expression's type is.

```
1 (let variable = e1:t1 in e2:t2):t2
```

We can of course nest these, and since data is immutable in OCaml, variables are overshadowed.

```
1 (* scoping.ml *)
2 let x = 3 in let y = 4 in x + y (* 7 *)
3 let x = 3 in let x = 4 in x (* 4 *)
4 let x = 3 in let z = 4 + x in let x = 1 in x + z (* 8 *)
5 (* implicit parenthesis *)
6 let x = 3 in (let z = 4 + x in (let x = 1 in x + z))
```

³Technically, everything is an expression due to specifications of OCaml, but in the broad scheme of things, I don't like this.

⁴Technically it is an expression (by ocaml specs), but is not the same as the other expressions we talk about;Languages like Scheme or Racket would not consider this to be an expression

Here, whenever we look consider a variable's value, it is always the closest preceding binding. Also, just to reiterate, these are expressions so something like the following is also possible:

Now that we have an an idea of what an expression is and how to determine some basic values and types, we can build larger expressions. I think of this as analogous as taking statement variables p and p and then building larger statements like $p \lor q$. And since we know how to evaluate basic expressions and find out their types and values, it's like knowing the truth values of p and q and being able to then conclude the truth value of $p \lor q$.

1.3.4 The if Expressions

Let us consider the very basic if expression. Now the if expression is an expression which means it has a value and type. But first let us consider it's syntax.

```
(if e1:bool then e2:t e3:t):t
```

What does this mean? As stated before, I will be using e to represent expressions and t for types, with e:t meaing that e has type t. So in this case, the if expression has an expression e1 which must evaluate to a bool, and two other expressions e2 and e3 which must **both** evaluate to the same type t. The if expression as a whole then has that same type t. A little weird, let's see an example.

```
1 if true then 3 else 4
```

Here true is an expression of type bool and both 3 and 4 are expressions of type int which means this expression as a whole has type int. Now because we can substitute any valid expression for e1, e2, e3 as long as their types follow the above rules all the following are valid expressions:

```
1 if true then 3 else 4
2 if true then false else true
3 if 3 < 4 then 5 + 6 else 7 + 8
4 if (if true then false else true) then (if false then 3 else 4) else (if true then 5 else 6)</pre>
```

Unlike Python or C, the only things that evaluate to bools are true and false or expressions that evaluate to true and false. So if 3 then 4 else 5 would be invalid. This idea of substituting any expression with the expected type can be used for any expression that has 'subexpressions'. So the following are valid with let bindings and let expressions:

```
1 let x = if true then false else true
2 let y = 3 + 4 - 10 in if true then y else y + 10
```

1.3.5 Functions as Expressions

We stated earlier that functional programming is one where we want to be able to treat functions as data. We have actually kinda saw this before. Consider the following:

There is not much difference here as what is printed out or how we use the name x. In OCaml, I consider variables to be functions with no parameters that return a value very much like our x method above. This is because at the end of the day, if we recall out C and 216 days, a variable is just a way to refer to some specific memory address that holds data. That data could be a value, could be code. But an actual function definition looks like this:

```
1 (* functions.ml *)
2 let area l w = l * w
3 (* or to use a let expression where we call the function *)
4 let area l w = l * w in area 2 3
5 (* syntax *)
6 (* (let name e1:t1 e2:t2 ... ex:tx = e:ty):t1 -> t2 -> tx -> ty *)
```

Like let bindings a function definition by itself is not an expression. You will need the in keyword if you want it to be an expression. The type of a function is represented as a list of types that looks like $t1 -> t2 -> \ldots -> tx -> ty$, For example let area l w = l * w in area has type int -> int. The last type in this list is always the return type, where the preceding types are the types for input.

The fun part is that since we know functions are expressions, and functions can take in expressions as input, then we can have functions that take in other functions.

```
1 (* functional1.ml *)
2 let area l w = l * w (* int -> int -> int *)
3 let apply f x y = f x y (* ('a -> 'b -> 'c) -> 'a -> 'b -> 'c *)
4 apply area 2 3
5 (* optional parenthesis *)
6 (* apply (area) (2) (3) *)
```

Now we have some new things to talk about here. Namely, what is 'a, 'b, 'c and why is area's type int -> int -> int and not something like float -> float -> float?

1.3.6 Type Inference

Let us consider the area function: let area l w = l * w. OCaml knows that this is a function with type int -> int. Which means we cannot do something like area 2.3 4.5. Why is this and how does this work?

Type inference is a way for a programming language to determine the type of a variable or value. In some languages it's real easy because you explicitly declare types: int x = 3;. In OCaml, variables types are determined by the operations or syntax of the expression. So just like you can only use things like && and | | on bools, we can only use things like +, -, *, on ints. If you wanted to do operations on floats then you need to use different operators. See the following:

```
1  (* operations.ml *)
2  2 + 3 (* int and int *)
3  1.3 +. 4.3 (* float and float *)
4  "hello" ^ " world" (* string and string *)
5  true || false (* bool and bool *)
6  int_of_char 'a' (* char input, int output *)
7  2 + 3.0 (* error *)
8  3 ^ 4 (* error *)
```

Some operators however, work on many different types. One such example is the > (greater than) operator. This operator along with <, >=, <=, = all can take in any two inputs as long as those two inputs are the same type. The output will always be of type bool.

```
1 (* compare.ml *)
2 2 > 4 (* false *)
3 "hello" <= "world" (* true *)
4 true = false (* false *)</pre>
```

One thing to note is that we use = for testing equality since we bind variables with let $\dots = e$. So we can say something like let x = 2 = 3 and OCaml knows that x is the variable and anything after the first = sign is the expression. Anyway, this is important because then what type is inferred from a function like

```
1 (* typeInference0.ml *)
2 let compare x y = x > y in compare
```

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Here we have no idea what type x and y have to be. In this case, OCaml uses a special type notation. The type of compare is 'a -> 'a -> bool. That is, we have two inputs which must both be the same type, and we know the result will be of type bool. If we are given something even stranger like:

```
1 (* typeInference1.ml *)
2 let f x y = 3
3 (* this is equivalent to something like
4 def f(x,y)
5     3
6 end
7 *)
```

OCaml will give this function type 'a -> 'b -> int. We are returning an int but the input types could be anything. Since the input types don't even need to be the same type here, we give them different symbols. So let's go back to our apply function and break it's type down again.

```
1 (* typeInference2.ml *)
2 let apply f x y = f x y in apply (* ('a -> 'b -> 'c) -> 'a -> 'b -> 'c *)
```

First let's list out the parameter names: f, x, y. The first parameter is a function which has two inputs of unknown type. We also don't know if the two inputs have to be the same or different. At this moment we know that the function's type is 'a -> 'b -> ?. Looking at the function we are given no information about what the return type of f is so we give it yet a another symbol. Thus we can say that the type of f is 'a -> 'b -> 'c. Now we know that f is being called on parameters f and f so we know that f must be the type of f 's first argument so we can give f type 'a. We then know that f is being used as f 's second argument so it should be of type 'b. So at this point we know the type of apply is ('a -> 'b -> 'c) -> 'a -> 'b -> ? (we put any function's type in parenthesis to show it's a function). Lastly we know that the returned value of apply is whatever f f f f returns. Since we know that f returns some value of type 'c, we can say apply's return type is also 'c. Thus the entire type of apply is ('a -> 'b -> 'c) -> 'a -> 'c)

1.4 Ocaml Pattern Matching

The next feature that OCaml allows us to have is the ability to pattern match. Pattern matching is, if you squint, very closely related to a switch statement. While I could show you pattern matching with what we know, I find it easier to demonstrate once we know OCaml's built in data structure: lists.

1.4.1 Lists

In other languages you may used to having these data structures called Arrays. In OCaml we don't have arrays, we what we have instead is lists. Let's first see the syntax:

```
1 (* list.ml*)
2 [1;2;3;4] (* type: int list *)
3 (* syntax *)
4 (* [el:t; e2:t; ... ex:t]*)
```

Looks a little like an Array but instead of being comma delimited, it is semi-colon delimited. Looking at the syntax we can also conclude that the lists must be homogeneous. Additionally, we can see that we do not need to put values, but rather we can put expressions. Here are some examples of other lists

```
1 (* list1.ml*)
2 [1;2;3;4] (* int list *)
3 [2.3;1.0] (* float list *)
4 ["hello", "World"] (* string list *)
5 [2 + 3; 4-4; 7 * 9] (* int list *)
6 let f1 x = x + 1 in let f2 y = x + 1 in let f3 z = z + 1 in [f1;f2;f3] (* (int -> int) list *)
```

The last one is a list of int -> int functions, wild huh? Now it is important to note that lists are implemented as a linked list under the hood which means they are recursive.

1.4.2 Recursion

Now you may have noticed that I have not talked about for, while, do while or any other type of looping structure. That is because it does not exist in OCaml. We have something better: recursion. In OCaml, data structures are recursive and to do looping, we need to make recursive functions. We will talk about this is a bit. We first need to talk about lists. Now since lists are recursive, we need to consider how to define a list. If you recall from 132 your linked list data structure, you should recall that a linked list in Java is a 'node' which contains a piece of data and then points to another list or null. In OCaml, we don't use these words, but they can be used analogously. In OCaml we don't point to Null, but instead we point to an empty list which we call Nil. We then have an element which points to the rest of the list, which we use what we call the Cons operator.

```
1 [] (* Nil, the empty list *)
2 1 :: [] (* 1 cons Nil, add 1 to the empty list. Evaluates to [1] *)
3 1 :: 2 :: [] (* 1 cons 2 cons NIL. Evaluates to [1;2] *)
4 1 :: [2] (* 1 cons list of 2. Evaluates to [1;2] *)
5 (* syntax *)
6 (* el:t :: e2:t list *)
```

Notice that the syntax shows that we are using expressions which means we have some wierd expressions that represent lists. Also note that the cons operator's left hand operator is of type t and the right hand operator must be of type t list.

```
1 [2 + 3; 4 - 5] (* int list. Evaluates to [5;-1] *)
2 [if true then false else true; false;] (* bool list. Evaluates to [false;false] *)
3 [[1;2;3];[4;5;6]] (* int list list. Is a value *)
4 [print_string "hello"; print_string "world"] (* Unit List. Don't worry about Unit now, but notice that "worldhello" is printed. *)
```

Notice that when we put expressions into lists, they are evaluated and not stored as expressions, but also evaluated from right to left order (see the last example).

1.4.3 Pattern Matching

So now that we have an idea of what a list is and how to construct one, now we have to learn how to deconstruct a list. Pattern matching is the way to deconstruct any data structure in OCaml and is a language feature not found in all languages. In order to pattern match, we need to learn a new expression: the match expression.

```
let x = 5
   match x with
       0 -> 0
3
       |1 -> 1
4
       |3 -> 2
5
6
       |5 -> 3
       |_ -> 4
7
   (* Syntax *)
   (* (match e1:t1 with
9
10
        pattern1 -> e2:t2
        |pattern2 -> e3:t2
11
        | ... ):t2
12
```

A match expression takes in an expression/value and then checks to see if it has the same structure as any of the cases. If it matches with a case, it will then preform the expression linked to the case. The last line is an underscore, which is used as a wildcard (match with anything else). Here is an analogous switch statement:

```
switch(5){
   case(0): return 0;
   case(1): return 1;
   case(3): return 2;
```

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```
case(5): return 3;
default: return 4;
}
```

I don't want you to think of them as the same though, and pattern matching can do a lot more than a switch statement so just use this vaguely related but not the same. However like a switch statement, a match statement will check until the first pattern that satisfies the requirements and then not look at any of the other patterns. Additionally, notice the match expression is an expression which means it can be evaluated to a value and has a type. It's type is whatever each case returns, and so we need each branch to have the same return type. The next thing to discuss is the idea of a pattern. A pattern is not like a regular expression pattern, but it matches with how a piece of data could be represented. Consider all the ways we can represent a list of 2 items. We can use each of these in a math expression and they mean the same thing.

```
1 match [1;2] with
2 a::b::[] -> 0
3 |a::[b] -> 1
4 |[a;b] -> 2
```

In the above example, the expression evaluates to 0, but all of those patterns mean the same thing. Here is an example of pattern matching on a list where we return the length or 4 if longer than 3 elements.

```
1 (*let lst = ... some list *)
2 match lst with
3    [] -> 0
4    |[a] -> 1
5    |a::b::[] -> 2
6    |a::[b;c] -> 3
7    |h::t -> 4
```

In this example we are matching some previously defined list named lst and seeing if the structure is anything like what we have on lines 3-7. If we take a look at line 7, we will see this pattern h::t. Remember our syntax of a list: e1:t :: e2:t list. This pattern is just a single value cons to some list of some arbitrary size. Ultimately, as long as a list's size is greater than 1, this pattern would match, but since it's the last item, it will only be reached if the preceding patterns do not match.

1.4.4 Recursive Functions

Knowing all this, we can then make functions that find the head of a list, or the last item of a list, but first remember what I said earlier, there is no looping construct except recursion. So we need to make recursive functions. To make a recursive function is the same as how we construct any other function but we need the rec keyword. Let's unalive 2 creatures with 1 weapon:

```
1 (* Assume the list cannot be empty *)
2 let rec tail lst = match lst with
3    [x] -> x
4    |_::t -> tail t
```

First, notice a recursive function is similar to a normal function. We just need the rec keyword after the let keyword. Next, let's consider the patterns I used. If we assume the list is not empty, then the base case is a list with 1 item. In this case, just return that 1 item. Otherwise, if the list takes the form of _::t, or something cons list, then just recursively call tail on the rest of the list. Notice that since I did not need the head item, I did not need to bind it to a variable, so I could just use the wildcard character. Another recursive function example: sum up the values in an int list.

```
1 let rec sum lst = match lst with
2   [] -> 0
3   |h::t -> h + sum t
```

There are other data types that exist besides lists which you can use and pattern match on. Please refer to the Data Types and Syntax section for more (Section 1.5).

1.5 Data Types and Syntax

1.5.1 Data Types

Basic Types

There are a few basic types in OCaml that we cover in this course. They are:

- int
- · float
- bool
- string
- char

Data Structures

There are 4 main data structures that exist in OCaml. They are

- Lists
- Tuples
- Variants
- · Records

. Each one of these things can be pattern matched and used to construct more complicated data structures. However in my experience I have rarely ever used records.

I talked about lists in an earlier section of this chapter so you can refer there for more info but here are some examples.

```
1 [1;2;3] (* int list*)
2 [] (* empty list, Nil, 'a lst *)
3 [2.0 +. 3.4] (* float list *)
4 let f x = x + 1 in let g y = y * 1 in [f;g] (* (int -> int) list *)
```

Now that we are refreshed on lists, let's talk about tuples. Tuples are ways for us to package data together to be a single 'value' so to speak. This can be useful since functions can only have one return value, so if we need to return multiple pieces of data, a tuple could be the way to go. But enough talking, here is an example:

```
1 (* tuples.ml *)
2 (3,4) (* int * int *)
3 (1,2,"hello") (* int * int * string *)
4 (* syntax *)
5 (* (e1:t1,e2:t2,...,ex:tx):t1 * t2 * ... tx *)
```

As you can see tuples are just expressions that comma delimited and placed in parenthesis. Some important things to note is that tuples are of fixed size and their type is dependent on the size and types of the subexpressions. For example, (3,2) is an int * int tuple which is different than 3,2,1) which is an int * int tuple. We can pattern match to break apart tuples by using our match expression.

```
1 (* tuple-match.ml *)
2 let t = (1,2)
3 match t with
4 |(0,0) -> 0
5 |(1,1) -> 1
6 |(1,b) -> b + b
7 |(a,b) -> a * b
```

1.5. DATA TYPES AND SYNTAX

The next data type we can talk about are variants. These are similar but not the same as enums. They are ways we can give names and make our own types in OCaml.

```
1 (* variants.ml *)
2 type coin = HEADS | TAILS
3 let x = HEADS (* type is coin, value is HEADS *)
```

These types are then recognized by the rest of OCaml and we can write functions based on these types. To figure out what type you are using, you can use pattern matching.

```
1 (* variants.ml *)
2 type coin = HEADS | TAILS
3 let flip c = match c with HEADS -> TAILS | TAILS -> HEADS
4 (* flip is a function of type coin -> coin *)
5 type parity = Even | Odd
6 let is_even p = match p with Even -> true | Odd -> false
7 (* is_even is a function of type parity -> bool *)
```

These variants are helpful for just renaming or making data values look pretty. For each of these examples we could have just used bools or ints to represent data. However, variants also allow us to store data in our custom types. Consider the following:

```
1 (* variants.ml *)
2 type shape = Rect of int * int | Circle of float
3 let r = Rect 3 4 (* type is shape, value is Rect(3,4) *)
4 let c = Circle 4.0 (* type is shape, value is Circle(4.0) *)
```

Here I am saying to make a shape type and that shapes can either be Rects which hold int * int tuple information, or Circles which hold floats. We can pattern match to figure out what type we are talking about, and to pull out information.

```
1 (* variants.ml *)
2 type shape = Rect of int * int | Circle of float
3 let r = Rect 3 4 (* type is shape, value is Rect(3,4) *)
4 let c = Circle 4.0 (* type is shape, value is Circle(4.0) *)
5 let area s = match s with
6 Rect(l,w) -> float_of_int l * w (* need to cast this to float so return types match *)
7 | Circle(r) -> r * r * 3.14
```

This is useful if we want to make Trees or our own lists.

The last data type we will cover here are records. They are groupings of key-value pairs. Records are basically named tuples, however the order does not matter in them, because the names of the keys will be the basis for lookup, rather than position.

```
(* Records *)
type date = {month:string; day:int; year:int}
let today = {day=29;Month="feb";year=3000}
```

When you define a record type, you say the names of the keys followed by the type of data they map to. Once you define a record, you cannot add or remove the key names. Additionally, when you initialize a record, you have to give a value for

every key, as there is not a default value that can be used upon creation. However, notice the order of key-values used in the tuple does not matter.

The cool thing is that records can access thier values when

1.5.2 Syntax

This is more a cheat sheet of basic/common expressions used in this course and their types.

```
int functions
(e1:int + e2:int): int
                                     (e1:int - e2:int): int
(e1:int / e2:int): int
                                     (e1:int * e2:int): int
float functions
(e1:float +. e2: float): float
                                     (e1:float -. e2: float): float
(e1:float /. e2: float): float
                                     (e1:float *. e2: float): float
bool functions
(e1:bool && e2:bool): bool
                              if expressions
(if e1:bool then e2:t else e3: t): t
let expressions
(let var = e1:t1 in e2: t2):t2
(let [rec] name arg1:t1 arg2:t2 ... argx:tx = e0:t0 in name): t1 -> t2 -> ... -> tx -> t0
pattern matching
(match e1:t1 with
  p1 -> e2: t2
| p2 -> e3: t2
| px -> ex: t2): t2
List and Tuple Creation
(e1:t1, e2:t2, ..., ex:tx): t1 * t2 * ... * tx
[e1:t; e2:t; ...; e3:t]: t list
List Operations
(e1:t :: e2: t list): t list
(e1:t list @ e2: t list): t list
```